

## **nat\_extra**<sup>4,23</sup>

STM: id\_increasing

STM: increasing\_implies

STM: increasing\_implies\_le

STM: compose\_increasing

STM: increasing\_inj

STM: increasing\_le

STM: increasing\_is\_id

STM: increasing\_lower\_bound

STM: injection\_le

STM: disjoint\_increasing\_onto

STM: bijection\_restriction

ABS:  $\text{primrec}(n;b;c)$  **primrec**

STM: primrec\_wf

STM: primrec\_add

ABS:  $\text{nondecreasing}(f;k)$  **nondecreasing**

STM: nondecreasing\_wf

STM: const\_nondecreasing

ABS:  $\text{fadd}(f;g)$  **fadd**

STM: fadd\_wf

STM: fadd\_increasing

ABS:  $\text{fshift}(f;x)$  **fshift**

STM: fshift\_wf

STM: fshift\_increasing

ABS:  $\text{finite}(T)$  **finite**

STM: finite\_wf

STM: nsub\_finite  
ABS:  $f[n:=x]$  **fappend**  
STM: fappend\_wf  
STM: increasing\_split  
ABS:  $\text{sum}(f(x) \mid x < k)$  **sum**  
STM: sum\_wf  
STM: non\_neg\_sum  
STM: sum\_linear  
STM: sum\_scalar\_mult  
STM: sum\_constant  
STM: sum\_functionality  
STM: sum\_difference  
STM: sum\_le  
STM: sum\_bound  
STM: sum\_lower\_bound  
STM: sum-ite  
STM: sum\_arith1  
STM: sum\_arith  
STM: finite-partition  
STM: pigeon-hole  
STM: isolate\_summand  
STM: empty\_support  
STM: singleton\_support\_sum  
STM: pair\_support  
STM: sum\_split  
ABS:  $\text{sum}(f(x;y) \mid x < n; y < m)$  **double\_sum**  
STM: double\_sum\_wf

STM: pair\_support\_double\_sum  
STM: double\_sum\_difference  
STM: double\_sum\_functionality  
ABS:  $R^n$  **rel\_exp**  
STM: rel\_exp\_wf  
STM: decidable\_rel\_exp  
STM: rel\_exp\_add  
ABS:  $R_1 \Rightarrow R_2$  **rel\_implies**  
STM: rel\_implies\_wf  
STM: rel\_exp\_monotone  
ABS:  $R$  preserves  $P$  **preserved\_by**  
STM: preserved\_by\_wf  
STM: preserved\_by\_monotone  
ABS: when  $P$ ,  $R_1 \Rightarrow R_2$  **cond\_rel\_implies**  
STM: cond\_rel\_implies\_wf  
STM: cond\_rel\_exp\_monotone  
ABS:  $R^*$  **rel\_star**  
STM: rel\_star\_wf  
STM: rel\_star\_monotone  
STM: cond\_rel\_star\_monotone  
STM: rel\_star\_transitivity  
STM: rel\_star\_monotonic  
STM: cond\_rel\_star\_monotonic  
STM: preserved\_by\_star  
STM: rel\_star\_closure  
STM: rel\_star\_closure2  
STM: rel\_star\_of\_equiv

STM: cond\_rel\_star\_equiv  
 STM: rel\_rel\_star  
 STM: rel\_star\_trans  
 STM: rel\_star\_weakening  
 ABS:  $R^{-1}$  **rel\_inverse**  
 STM: rel\_inverse\_wf  
 STM: rel\_inverse\_exp  
 STM: rel\_inverse\_star  
 STM: rel\_star\_symmetric  
 STM: rel\_star\_symmetric\_2  
 STM: preserved\_by\_symmetric  
 ABS:  $R_1 \vee R_2$  **rel\_or**  
 STM: rel\_or\_wf  
 STM: rel\_implies\_or\_left  
 STM: rel\_implies\_or\_right  
 STM: symmetric\_rel\_or  
 STM: preserved\_by\_or  
 ABS:  $P$  as strong as  $Q$  **as\_strong**  
 STM: as\_strong\_wf  
 STM: as\_strong\_transitivity  
 ABS:  $f^n$  **fun\_exp**  
 STM: fun\_exp\_wf  
 STM: comb\_for\_fun\_exp\_wf  
 STM: fun\_exp\_compose  
 STM: fun\_exp\_add  
 STM: fun\_exp\_add1  
 STM: fun\_exp\_add1\_sub

STM: iteration\_terminates

ABS:  $(i, j)$  **flip**

STM: flip\_wf

STM: sum\_switch

STM: flip\_symmetry

STM: flip\_bijection

STM: flip\_inverse

STM: flip\_twice

ABS:  $\text{search}(k;P)$  **search**

STM: search\_wf

STM: search\_property

STM: search\_succ

ABS:  $P \wedge Q$  **prop\_and**

STM: prop\_and\_wf

STM: and\_preserved\_by

ABS: (ternary)  $R$  preserves  $P$  **preserved\_by2**

STM: preserved\_by2\_wf

STM: and\_preserved\_by2